

Section 8.2 Zero and Negative Exponents

Assignment:

Definition of Zero and Exponents

Let a be a non-zero number and let n be a positive integer.

*** A non-zero number to the zero power is 1.

$$a^0 = 1, a \neq 0$$

*** a^{-n} is the reciprocal of a^n

$$a^{-n} = \frac{1}{a^n}, a \neq 0$$

Examples

1.

a. $\frac{3^{-4}}{1} = \frac{1}{3^4} = \frac{1}{81}$

c. $\frac{4^{-2}}{1} = \frac{1}{4^2}$

e. $0^{-1} = \frac{1}{0} = \text{und.}$

$$(x^3 + 4z^7)^0 = 1$$

b. $(-5.2)^0 = 1$

d. $(\frac{3}{5})^{-1} = \frac{5}{3}$

2. Rewrite with positive exponents. Assume k is positive.

a. $(3x^{-2})^3 = \frac{3^3 x^{-6}}{x^6} = \frac{27}{x^6}$

b. $5g^{-3}h^{-4} = \frac{5}{g^3 h^4}$

3. Evaluate the expression.

a. $4^{-3}4^3$ $4^0 = 1$

b. $(5^{-2})^{-3}$ $5^6 = 15625$

c. 2^{-3} $\frac{1}{2^3} = \frac{1}{8}$

4. Rewrite with positive exponents. Assume n is positive.

a. $(4y^4)^{-3}$ $\frac{1}{(4y^4)^3} = \frac{1}{64y^{12}}$

b. $\frac{1}{a^{-2n}}$ a^{2n}

$$P = 5325(1.02)^t$$

5. Census figures showed that a town's population can be modeled by $P = 5325(1.02)^t$, where $t=0$ represents the year 2010.

a. Estimate the population in the year 1999.

$t = -11$ $P = 5325(1.02)^{-11}$
 $P = \frac{5325}{(1.02)^{11}}$ $P \approx 4282.7$

b. Estimate the population in the year 2010.

$t = 0$ $P = 5325(1.02)^0$
 $P = 5325$