

Section 8.5 Exponential Growth Functions

Assignment:

Exponential Growth increases at the same rate over a unit of time.

Exponential Growth Model

$$y = C(1+r)^t$$

C = initial amount

r = rate (dec.)

$(1+r)$ = growth factor

t = time based on compounding.

Examples

1. A savings certificate of \$1000 pays 6.5% annual interest compounded yearly. What is the balance when the certificate matures after 5 years?

$$C = \$1000$$

$$r = 6.5\% = .065$$

$$(1+r) = 1.065$$

$$t = 5 \text{ years}$$

$$y = 1000(1.065)^5$$

$$y \approx \$1370.09$$

2. You deposit \$800 in a savings account that pays 2.5% annual interest compounded yearly. What is the balance after 3 years?

$$C = 800$$

$$r = .025$$

$$r+1 = 1.025$$

$$t = 3$$

$$C = 800(1.025)^3$$

$$C \approx \$861.51$$

3. An experiment started with 100 bacteria. They double in number every hour.

- a. Write a model for the number of bacteria after 8 hours.

$$C = 100$$

$$r = 1$$

$$1+r = 2$$

$$t = 8$$

$$y = 100(2)^8$$

$$y = 100(2)^t$$

- b. Find the number of bacteria after 8 hours.

$$y = 25,600 \text{ bacteria}$$

Section 8.6 Exponential Decay Functions

Assignment:

Exponential Decay

decreases the same amount
for a unit of time

Exponential Decay Model

$$y = C(1-r)^t$$

C = initial

r = rate

$(1-r)$ = decay factor

t = time

Examples

1. From 1983 to 1997, the ratio of students per computer at a school has dropped by about 16.8% per year. If there were 103 students per computer in 1983 and 1983 is the base for comparison, what was the number of students per computer in 1997?

$$\begin{aligned} C &= 103 \\ r &= .168 \\ 1-r &= .832 \\ t &= 14 \end{aligned}$$

$$\begin{aligned} t &= 0 \text{ in } 1983 \\ t &= 14 \text{ in } 1997 \\ y &= 103(.832)^{14} \\ y &= 8 \text{ students} \end{aligned}$$

2. You bought a used boat for \$2300. The value of the boat will be less each year because of depreciation. The boat depreciates at the rate of 8% per year.

a. Write an exponential decay model to represent this situation.

$$\begin{aligned} C &= 2300 \\ r &= .08 \end{aligned}$$

$$\begin{aligned} 1-r &= .92 \\ t &= t \end{aligned}$$

$$y = 2300(.92)^t$$

b. Estimate the value of the boat in 2 years.

$$t = 2$$

$$\begin{aligned} y &= 2300(.92)^2 \\ y &\approx \$1946.72 \end{aligned}$$

c. Estimate the value of the boat in 5 years.

$$t = 5$$

$$\begin{aligned} y &= 2300(.92)^5 \\ y &\approx \$1518.89 \end{aligned}$$