

# Chapter 6

## Solving and Graphing Linear Inequalities

## Section 6.1 Solving One-Step Linear Inequalities

Graph of a linear inequality in one variable is all the solutions that satisfy the inequality are graphed on a # line

### EXAMPLES

1. Write the linear inequality and draw the graph for each verbal phrase.

- \*\*\* An open dot is used for  $<$  and  $>$ .  
 \*\*\* A closed dot is used for  $\leq$  and  $\geq$ .

Verbal Phrase	Inequality	Graph
a. All real numbers less than 2	$x < 2$	
b. All real numbers greater than -2	$x > -2$	
c. All real numbers less than or equal to 1	$x \leq 1$	
d. All real numbers greater than or equal to 1	$x \geq 1$	

2. John was sure that he didn't score less than 74 on his algebra test. Write an inequality to describe John's possible score. Graph the inequality.

$$x = \text{John's score}$$

$$x \geq 74$$

3. Solve each inequality and graph the solution on a number line.

\*\*\* Solving linear inequalities is similar to solving linear equations. To solve an inequality, isolate the variable by using transformations. However, when you multiply or divide each side of an inequality by a negative number, you must reverse the inequality symbol to maintain a true statement.

a.  $x + 8 \geq 1$   
 $-8 - 8$   
 $x \geq -7$

✓ if  $x=0$   
 $0 + 8 \geq 1$   
 $8 \geq 1$

b.  $3 < m - 5$   
 $m - 5 > 3$   
 $+5 +5$   
 $m > 8$

if  $m=10$   
 $3 < 10 - 5$   
 $3 < 5$

c.  $\frac{r}{2} < -2$   
 $r < -4$

if  $r=-6$   
 $\frac{-6}{2} < -2$   
 $-3 < -2$

d.  $-2.5y \geq 3$   
 $\frac{-2.5y}{-2.5} \frac{-2.5}{-2.5}$   
 $y \leq -1.2$

✓ if  $y=-2$   $-2.5(-2) \geq 3$   
 $5 \geq 3$

e.  $\frac{x}{3} \leq 15$  :3  
 $x \geq -45$   
 $0 \leq 15$   
 $0 \leq 15$

if  $x=0$

f.  $-42 > 14x$   
 $\frac{14x < -42}{14}$   
 $x < -3$

if  $x=-5$   
 $-42 > 14(-5)$   
 $-42 > -70$

