

# Chapter I

## Equations and Inequalities



## Section 1.1 Expression and Formulas

Variable: a letter in place of a number

Coefficient: a number multiplied to a variable

Constant: a number w/o a variable ( $x^0$ )

Algebraic Expression: a number sentence w/o an equal sign  
(can't be solved)

### Order of Operations - PEMDAS

1. Grouping / fraction bar
2. Exponents
3. mult / divide
4. Add / Subtract.

### **Let's Practice...**

**Evaluate each expression if  $a = -2$ ,  $b = 3$ , and  $c = 4$ .**

<p>1. <math>2a + (b+3)^2</math></p> <p><math>2(-2) + (3+3)^2</math></p> <p><math>-4 + (6)^2</math></p> <p><math>-4 + 36</math></p> <p><b>32</b></p>	<p>2. <math>a + 3(b^2 - (a+c))</math></p> <p><math>(-2) + 3(9 - (-2+4))</math></p> <p><math>-2 + 3(9 - 2)</math></p> <p><math>-2 + 3(7)</math></p> <p><math>-2 + 21</math></p> <p><b>19</b></p>	<p>3. <math>5c - 2[(b-a)+c]</math></p> <p><math>5(4) - 2[(3+2)+4]</math></p> <p><math>20 - 2(5+4)</math></p> <p><math>20 - 2(9)</math></p> <p><math>20 - 18</math></p> <p><b>2</b></p>
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Evaluate each expression if  $a = -2$ ,  $b = 3$ , and  $c = 4$ .

<p>4. <math>c(a^2 + b)</math></p> <p><math>4(4 + 3)</math></p> <p><math>4(7)</math></p> <p><math>28</math></p>	<p>5. <math>\frac{b^3 + ac}{ab + 2bc}</math></p> <p><math>\frac{27 + (-2)(4)}{(-2)(3) + 2(3)(4)}</math></p> <p><math>\frac{27 - 8}{-6 + 24}</math></p> <p><math>\frac{19}{18}</math></p>	<p>6. <math>\frac{9a - 2c}{4ab}</math></p> <p><math>\frac{9(-2) - 2(4)}{4(-2)(3)}</math></p> <p><math>\frac{-18 - 8}{-24}</math></p> <p><math>\frac{-26}{-24} = \frac{13}{12}</math></p>
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Let's practice...

A player's attack percentage  $a$  is calculated using the formula  $a = \frac{k - e}{t}$ , where  $k$  represents the number of kills,  $e$  represents the number of attack errors including blocks, and  $t$  represents the totals attacks attempted. Find the attack percentage given each set of values.

<p>7. <math>k = 22, e = 11, t = 35</math></p> <p><math>a = \frac{22 - 11}{35}</math></p> <p><math>a = \frac{11}{35}</math></p> <p><math>a \approx .31</math></p> <p><math>a \approx 31\%</math></p>	<p>8. <math>k = 33, e = 9, t = 50</math></p> <p><math>a = \frac{33 - 9}{50}</math></p> <p><math>a = \frac{24}{50}</math></p> <p><math>a = .48</math></p> <p><math>a = 48\%</math></p>
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## Section 1.2 Properties of Real Numbers

### Set of Real Numbers (R)

Natural numbers (N) Countable Numbers (No 0)  
 $\{1, 2, 3, \dots\}$

Whole numbers (W) includes 0  $\{0, 1, 2, 3, 4, \dots\}$

Integers (Z) N, W, includes negative #'s  $\{-2, -1, 0, 1, 2, \dots\}$

Rational numbers (Q) N, W, Z can be written as a fraction,  
 $\{-2, \frac{3}{4}, \sqrt[3]{3}, \sqrt{100}\}$

Irrational numbers (I) cannot be written as a fraction,  
 $\{\pi, \sqrt{2}, e\}$

Property	Addition	Multiplication
Commutative	$a + b = b + a$	$ab = ba$
Associative	$(a + b) + c = a + (b + c)$	$(ab)c = a(bc)$
Identity	$a + 0 = a$	$a(1) = a$
Inverse	Additive Inverse $a + (-a) = 0$	Multiplicative Inverse or Reciprocal $a \cdot \frac{1}{a} = 1 \quad a \neq 0$
Closure	$a + b = \mathbb{R}$	$a(b) = \mathbb{R}$
Distributive	$a(b + c) = ab + ac$	

**Let's practice ...**

Name the sets of numbers to which each belong.

62 $N, W, Z, Q, \mathbb{R}$	$\frac{5}{4}$ $Q, \mathbb{R}$	$\sqrt{11}$ $I$	-12 $Z, Q, \mathbb{R}$
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Name the property illustrated by each equation.

$(6 \cdot 8) \cdot 5 = 6(8 \cdot 5)$  Associative property of multiplication

$7(9 - 5) = 7 \cdot 9 - 7 \cdot 5$  Distributive

$84 + 16 = 16 + 84$  commutative property of +

The additive inverse of  $\frac{4}{9}$  is  $-\frac{4}{9}$ , the multiplicative inverse or reciprocal is  $\frac{9}{4}$ .

Simplify.

$3(2x - 4y) + 7(8x - 5)$

$6x - 12y + 56x - 5$

$61x - 12y - 5$

$-5(8x - 2y) - 4(-6x - 3y)$

$-40x + 10y + 24x + 12y$

$-16x + 22y$

### Section 1.3 Solving Linear Equations

Equation: # Sentence w/ = Sign (can be solved)

Sum: +

Difference: -

Product: (x) mult.

Quotient: ÷

Property	Examples
Reflexive	$a + b = a + b$
Symmetric	$a = b \quad b = a$
Transitive	if $a = b$ ; $b = c$ then $a = c$
Substitution	$a$ may be replaced $a = b$ ; $b = c$ then $a = c$ by replacement.

#### **Let's Practice...**

Write an algebraic expression to represent each verbal expression.

1. the product of 12 and the sum of a number and negative 3

$$12(n + (-3)) \quad \text{or} \quad 12(n - 3)$$

2. The difference between the product of 4 and a number and the square of the number.

$$4n - n^2$$

Write a verbal sentence to represent the following:  $\frac{x}{4} + 8 = -16$

the sum of 8 and the quotient of a number and four is -16.

Solve the equations.

1.  $\left(\frac{2}{9}x + 8 = 16\right) \times 9$

$$2x + 72 = 144$$

$$2x = 72$$

$$x = 36$$

2.  $12x - 3 = 4x + 21$

$$8x - 3 = 21$$

$$8x = 24$$

$$x = 3$$

3.  $5(x - 2) = 6 - (2x - 1)$

$$5x - 10 = 6 - 2x + 1$$

$$7x - 10 = 7$$

$$7x = 17$$

$$x = \frac{17}{7}$$

4.  $\left(\frac{2}{3}x + \frac{1}{4} = x - \frac{1}{6}\right) \times 12$

$$8x + 3 = 12x - 2$$

$$3 = 4x - 2$$

$$5 = 4x$$

$$x = \frac{5}{4}$$

5. Solve for  $q$  in the following equation:  $\left(\frac{8r - 5q}{2} = 3\right) \times 2$

$$8r - 5q = 6$$

$$\frac{-5q = 6 - 8r}{-5}$$

$$q = \frac{8r - 6}{5}$$



## Section 1.4 Solving Absolute Value Equations

The absolute value  $| \quad |$  of a number is the distance from 0 on a # line.

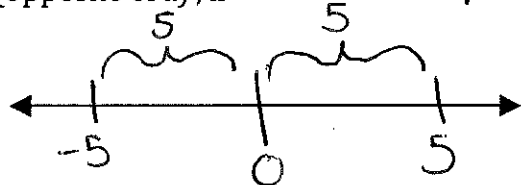
$$|a| = a, \text{ if } a \geq 0$$

$$|3| = 3$$

$$|a| = -a \text{ (opposite of } a), \text{ if } a < 0$$

$$|-3| = 3$$

$$|x| = 5$$



**Let's Practice...** Evaluate when  $x = -4$  and  $y = -9$ .

<p>a. <math> 4x + 3  - 7</math></p> $ 4(-4) + 3  - 7$ $ -16 + 3  - 7$ $ -13  - 7$ $13 - 7$ $\textcircled{6}$	<p>b. <math>-3 xy </math></p> $-3 -4(-9) $ $-3 36 $ $-3 \cdot 36$ $\textcircled{-108}$	<p>c. <math>-2 3x + 8  - 4</math></p> $-2 3(-4) + 8  - 4$ $-2 -12 + 8  - 4$ $-2 -4  - 4$ $-2(4) - 4$ $-8 - 4$ $\textcircled{-12}$
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<p>Solve: <math> 6x - 3  = 15</math></p> $6x - 3 = -15 \qquad 6x - 3 = 15$ $6x = -12 \qquad 6x = 18$ $x = -2 \qquad x = 3$ $x = \left\{ -2, 3 \right\}$	<p>Solve: <math>2 4x + 3  - 5 = 15</math></p> $2 4x + 3  = 20$ $ 4x - 3  = 10$ $4x - 3 = -10 \qquad 4x - 3 = 10$ $4x = -7 \qquad 4x = 13$ $x = -\frac{7}{4} \qquad x = \frac{13}{4}$ $x = \left\{ -\frac{7}{4}, \frac{13}{4} \right\}$
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## Section 1.5 Solving Linear Inequalities

**Important**

Multiplying or dividing each side of an inequality by a **negative** number requires you to **reverse** the inequality symbol.

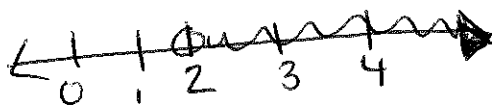
**Let's practice...**

Solve each inequality and graph the solution set on a number line.

a.  $11y - 9 > 13$

$$11y > 22$$

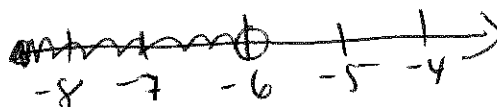
$$y > 2$$



b.  $-4w - 13 > -21$

$$-4w > 24$$

$$w < -6$$



c.  $7x + 9 \geq 10x - 12$

$$9 \geq 3x - 12$$

$$3x - 12 \leq 9$$

$$3x \leq 21$$

$$x \leq 7$$



d.  $\frac{2x - 9}{4} \leq x + 2$

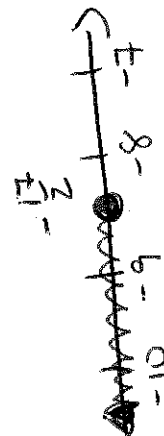
$$2x - 9 \leq 4x + 8$$

$$-9 \leq 2x + 8$$

$$2x + 8 \leq -9$$

$$2x \leq -17$$

$$x \leq \frac{-17}{2} \text{ or } -8.5$$



e. Tara is delivering bags of mulch. Each bag weighs 48 pounds and the push cart weighs 65 pounds. If her truck is capable of hauling 1 ton, how many bags of mulch can she safely take on each trip?  
 1 ton = 2000 lbs

$$48m + 65 \leq 2000$$

$$48m \leq 1935$$

$$\frac{48m}{48}$$

$$m \leq 40.3125$$

$$m \leq 40 \text{ bags}$$

## Section 1.6 Algebra Lab

### Set Builder Notation vs. Interval Notation

Open circle  $\rightarrow ( )$




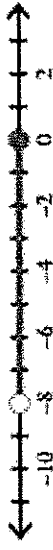
Closed circle  $\rightarrow [ ]$

If **or** is used, the union  $\cup$  symbol is used in place of **or**.

	Set Builder Notation	Interval Notation	Graph
1.	$\{x \leq -5\}$	$(-\infty, -5]$	
2.	$\{-9 < x < 7\}$	$(-9, 7)$	
3.	$\{x \geq -4\}$	$[-4, \infty)$	
4.	$\{x < 6 \text{ or } x > 8\}$	$(-\infty, 6) \cup (8, \infty)$	
5.	$\{x \leq -3 \text{ or } x \geq 5\}$	$(-\infty, -3] \cup [5, \infty)$	
6.	$\{4 < x < 9\}$	$(4, 9)$	

Algebra 2  
1.6 Notation Practice

Name \_\_\_\_\_

	Graph	Set Notation	Interval Notation
1.		$\{x \mid x < -10 \text{ or } x > 5\}$	$(-\infty, -10) \cup (5, \infty)$
2.		$\{x \mid 6 < x < 8\}$	$(6, 8)$
3.		$\{x \mid x < -2 \text{ or } x \geq 2\}$	$(-\infty, -2) \cup [2, \infty)$
4.		$\{x \mid -8 \leq x < 0\}$	$[-8, 0)$

## Section 1.6 Solving Linear Inequalities

**Important**

Multiplying or dividing each side of an inequality by a **negative** number requires you to **reverse** the inequality symbol.

### Part One: Compound Inequalities

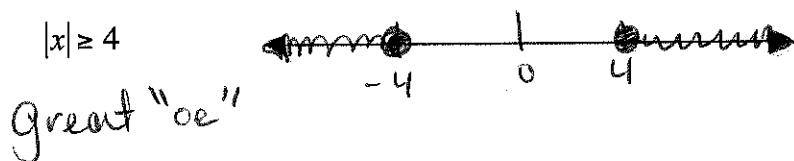
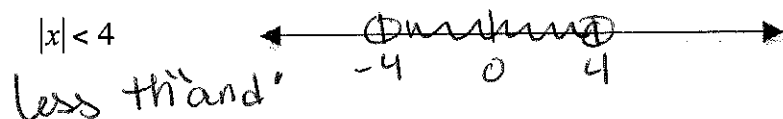
A compound inequality consists of two inequalities w/ the same variable separated by "and" or "or"

Let's practice...

Solve each inequality and graph the solution set on a number line.

<p>a. <math>-8 &lt; 3t + 4 &lt; 10</math></p> <p style="margin-left: 40px;">and</p> <div style="display: flex; justify-content: space-between;"> <div style="width: 45%;"> <math display="block">-8 &lt; 3t + 4</math> <math display="block">-12 &lt; 3t</math> <math display="block">-4 &lt; t</math> </div> <div style="width: 45%; border-left: 1px solid black; padding-left: 10px;"> <math display="block">3t + 4 &lt; 10</math> <math display="block">3t &lt; 6</math> <math display="block">t &lt; 2</math> </div> </div> <p style="text-align: center; margin: 10px 0;"><math>\{ -4 &lt; x &lt; 2 \}</math></p>	<p>b. <math>-5 \geq 3x - 2 &gt; -14</math></p> $-3 \geq 3x > -12$ $-1 \geq x > -4$ <p style="text-align: center; margin: 10px 0;"><math>\{ -4 &lt; x &lt; -1 \}</math></p>
<p>c. <math>-2x + 7 &lt; 3</math> or <math>3x + 5 &lt; 2</math></p> <div style="display: flex; justify-content: space-between;"> <div style="width: 45%;"> <math display="block">-2x &lt; -4</math> <math display="block">x &gt; 2</math> </div> <div style="width: 45%; border-left: 1px solid black; padding-left: 10px;"> <math display="block">3x &lt; -3</math> <math display="block">x &lt; -1</math> </div> </div> <p style="text-align: center; margin: 10px 0;"><math>\{ x &lt; -1 \text{ or } x &gt; 2 \}</math></p>	<p>d. <math>5x \geq 15</math> or <math>-3x \geq 21</math></p> $x \geq 3 \text{ or } x \leq -7$ <p style="text-align: center; margin: 10px 0;"><math>\{ x \leq -7 \text{ or } x \geq 3 \}</math></p>

## Part Two: Absolute Value Inequalities



Let's practice...

Solve each absolute value inequality.

a.  $|4x-7| - 2 > 17$  "or"

$$|4x-7| > 19$$

$$4x-7 > 19 \quad \text{or} \quad 4x-7 < -19$$

$$4x > 26 \quad \quad \quad 4x < -12$$

$$x > \frac{26}{4} \quad \quad \quad x < -3$$

$\left\{ x \mid x > \frac{13}{2} \text{ or } x < -3 \right\}$

b.  $|5x-2| + 3 < 17$  "or"

$$|5x-2| < 14$$

$$5x-2 > -14 \quad \text{or} \quad 5x-2 < 14$$

$$5x > -12 \quad \quad \quad 5x < 16$$

$$x > -\frac{12}{5} \quad \quad \quad x < \frac{16}{5}$$

$\left\{ x \mid x > -\frac{12}{5} \text{ or } x < \frac{16}{5} \right\}$

c.  $|-6b| \leq 60$  "and"

$$-60 \leq -6b \leq 60$$

$$10 \geq b \geq -10$$

$\left\{ -10 \leq b \leq 10 \right\}$

d.  $2|4x+3| - 5 > 15$  "and"

$$2|4x+3| > 20$$

$$|4x+3| > 10$$

$$-10 < 4x+3 < 10$$

$$-13 < 4x < 7$$

$\left\{ -\frac{13}{4} < x < \frac{7}{4} \right\}$